

Electron-phonon : let us define

$$g_{\mathbf{q}\nu}(\mathbf{k}, i, j) = \left(\frac{\hbar}{2M\omega_{\mathbf{q}\nu}} \right)^{1/2} \langle \psi_{i,\mathbf{k}} | \frac{dV_{SCF}}{d\hat{u}_{\mathbf{q}\nu}} \cdot \hat{\epsilon}_{\mathbf{q}\nu} | \psi_{j,\mathbf{k}+\mathbf{q}} \rangle. \quad (1)$$

The phonon linewidth $\gamma_{\mathbf{q}\nu}$ is defined by

$$\gamma_{\mathbf{q}\nu} = 2\pi\omega_{\mathbf{q}\nu} \sum_{ij} \int \frac{d^3k}{\Omega_{BZ}} |g_{\mathbf{q}\nu}(\mathbf{k}, i, j)|^2 \delta(e_{\mathbf{q},i} - e_F) \delta(e_{\mathbf{k}+\mathbf{q},j} - e_F), \quad (2)$$

while the electron-phonon coupling constant $\lambda_{\mathbf{q}\nu}$ for mode ν at wavevector \mathbf{q} is defined as

$$\lambda_{\mathbf{q}\nu} = \frac{\gamma_{\mathbf{q}\nu}}{\pi\hbar N(e_F)\omega_{\mathbf{q}\nu}^2} \quad (3)$$

where $N(e_F)$ is the DOS at the Fermi level. The spectral function is defined as

$$\alpha^2 F(\omega) = \frac{1}{2\pi N(e_F)} \sum_{\mathbf{q}\nu} \delta(\omega - \omega_{\mathbf{q}\nu}) \frac{\gamma_{\mathbf{q}\nu}}{\hbar\omega_{\mathbf{q}\nu}}. \quad (4)$$

The electron-phonon mass enhancement parameter λ can also be defined as the first reciprocal momentum of the spectral function:

$$\lambda = \sum_{\mathbf{q}\nu} \lambda_{\mathbf{q}\nu} = 2 \int \frac{\alpha^2 F(\omega)}{\omega} d\omega. \quad (5)$$

Note that a factor $M^{-1/2}$ is hidden in the definition of normal modes as used in the code.

McMillan:

$$T_c = \frac{\Theta_D}{1.45} \exp \left[\frac{-1.04(1 + \lambda)}{\lambda(1 - 0.62\mu^*) - \mu^*} \right] \quad (6)$$

or (better?)

$$T_c = \frac{\omega_{log}}{1.2} \exp \left[\frac{-1.04(1 + \lambda)}{\lambda(1 - 0.62\mu^*) - \mu^*} \right] \quad (7)$$

where

$$\omega_{log} = \exp \left[\frac{2}{\lambda} \int \frac{d\omega}{\omega} \alpha^2 F(\omega) \log \omega \right] \quad (8)$$